

# I • STRICTLY INSCRIBED SIMILAR TRIANGLES

### Problem

Two triangles **ABC** and **XYZ** are *Similar* if their corresponding sides are proportional (or, equivalently if their corresponding angles are equal. We will say that **ABC** and **XYZ** are *Similar In Order*, if **A** corresponds to **X**, **B** corresponds to **Y** and **C** corresponds to **Z**. That is:

|AB| / |XY| = |BC| / |YZ| = |AC| / |XZ|,

where  $|\mathbf{MN}|$  denotes the length of the line from **M** to **N**.

Triangle XYZ is *Strictly Inscribed in* triangle ABC, if each vertex of XYZ lies in the interior (not at a vertex) of a different edge of ABC. This means that no edge of XYZ can be contained in an edge of ABC. If XYZ is similar in order to ABC and strictly inscribed in ABC, we say that XYZ is a *Strictly Inscribed Similar Triangle* to ABC.

If the line through  $\mathbf{X}$  and  $\mathbf{Y}$  makes an angle  $\mathbf{0}$  with the line through  $\mathbf{A}$  and  $\mathbf{B}$ , there are four possible orientations illustrated in the figures below.  $\mathbf{X}$  and  $\mathbf{Y}$  may be at either end of the segment and the third vertex,  $\mathbf{Z}$ , may be on either side of the line. In the figures, the line through  $\mathbf{X}$  and  $\mathbf{Y}$  makes an angle of  $\mathbf{30}^{\circ}$  with the line through  $\mathbf{A}$  and  $\mathbf{B}$ .



Depending on the shape of the outside triangle, **ABC**, and the angle,  $\theta$ , between the line through **X** and **Y** and the line through **A** and **B**, there may be 0, 1, 2, 3 or 4 strictly inscribed similar triangles to **ABC** with angle  $\theta$ .

Write a program, which takes as input the vertices of the triangle ABC and an angle  $\theta$ , and computes the vertices of all strictly inscribed similar triangles to ABC for which the line through X and Y makes an angle  $\theta$  with the line through A and B.



#### Notes

Use the value: **3.14159253** as the value for  $\pi$ , should you need it.

## Input

The first line of the input is a positive integer n which is the number of triangle datasets that follow. Each triangle dataset consists of four lines. The first line has the x and y coordinates of vertex A, the second line has the x and y coordinates of vertex B and the third line has the x and y coordinates of vertex C. The last line has the angle  $\theta$  in degrees between the line through X and Y and the line through A and B.

# Output

For each dataset, you will output the number of strictly inscribed similar triangles to **ABC** satisfying the input conditions. Then, for each such triangle, print a blank line, followed by a line containing the coordinates of vertex **X** (corresponding to **A**); a line containing the coordinates of vertex **Y** (corresponding to **B**); a line containing the coordinates of vertex **Z** (corresponding to **C**); and another blank line. Each coordinate should be given to four decimal places.

### Example

Input	Output
2	2
21 0 14 6 30 0 0	15.6030 4.6260 7.5905 0.0000 8.9396 3.8313
21 0 14 6 50	8.1575 0.0000 15.8312 4.4304 12.0075 5.1461
	1
	10.0510 0.0000 14.6315 5.4587 11.5450 4.9479